

# Understanding Educational Impacts: The Role of Literacy and Numeracy Skills

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# Introduction

- Substantial research on relationship between formal education and individual earnings
- Considerable evidence that schooling has a causal effect on earnings (Card, 1999, 2001)
- Large body of evidence on non-pecuniary impacts:
  - Recent surveys: Lochner (2011), Oreopoulos and Salvanes (2010)
  - Civic participation (Dee, 2004; Milligan, Moretti and Oreopoulos, 2004)
  - Health and longevity: mixed evidence (Lleras-Muney, 2005; Oreopoulos, 2007; Mazumder, 2008; Clark and Royer, 2013; Grossman, 2015)
  - Participation in crime (Lochner and Moretti, 2004)
  - Inter-generational impacts (Plug, 2004; Oreopoulos, Page and Stevens, 2006; Black, Devereux and Salvanes, 2005; Holmlund et al 2011)
  - Satisfaction with life (Oreopoulos, 2007)

# Motivation

- However, little known about mechanisms
- Possible schooling mechanisms:
  1. Education enhances cognitive skills
  2. Education improves non-cognitive skills
  3. Education (via improved earnings) alters budget constraint
  4. Education alters preferences (eg more 'forward looking')
- **Objective of paper:** assess extent to which impacts arise because of impact of schooling on basic literacy & numeracy skills and their consequences for individual outcomes

# Overview of Paper

- Study uses rich source of data that includes demographic and labour market information and results of cognitive skills tests (IALSS – Cdn component of Adult Literacy and Life Skills Survey)
- Data combine methods of educational testing with household survey techniques
- In IALSS 2003, skills were assessed in four domains:
  - Prose literacy, Document literacy, Numeracy, Problem-solving
- Provide measures of the skills of a representative sample of the adult population

- Key feature: these are skills used in daily activities – measures of job- and life-relevant skills, not ability measures
- eg: Document literacy: skills required to find and use information contained in text formats such as job applications, payroll forms, bus schedules, graphs
- Numeracy: “the knowledge and skills required to effectively manage and respond to the mathematical demands of diverse situations”
- Skills are assessed in English or French – i.e. correspond to “useable” skills in Canadian labour market

# Skills and Earnings: Interpretive Framework

- Simple framework builds on Welch (1969) and Rosen (1974).
- Hedonic model in which earnings are determined by the skills an individual possesses and the prices of those skills.

- Abstracting from other influences on earnings, individual earnings are a function of the skills an individual possesses and puts into use:

- $$E_i = f ( G_i^1 , G_i^2 , G_i^3 ) + e_i \quad (1)$$

- where  $E_i$  are earnings for individual  $i$ ,  $G_i^k$  is the amount of skill  $k$  that person  $i$  supplies in the market, and  $e_i$  is independent of the skills.

- Typically, we do not observe the skills but we do observe some of the inputs that generate them. They enter via skill production functions:

- $G_i^k = h_k( edn_i, exp_i, v_{ki} ) \quad (2)$

- where  $k$  indexes the skill type,  $edn$  corresponds to education,  $exp$  is years of work experience (or age) and  $v_k$  is an ability specific to the production of the  $k$ th skill.



- If we do not observe the  $G_i^k$  s directly, we can obtain an estimating equation by substituting equation 2) into 1).
- This yields a reduced form specification for earnings as a function of education and experience.
- The coefficient on a covariate  $x$  such as education (the “return” to schooling) reflects the combination of how that input contributes to production of each skill and how those skills contribute to earnings.

$$5) \frac{\partial E}{\partial x} = \frac{\partial f}{\partial G^1} * \frac{\partial h_1}{\partial x} + \frac{\partial f}{\partial G^2} * \frac{\partial h_2}{\partial x} + \frac{\partial f}{\partial G^3} * \frac{\partial h_3}{\partial x}$$

## What if some skills are observed?

- If we observe the cognitive skills  $G^1$ , we get a quasi-reduced form earnings regression that includes  $G^1$  (the vector of cognitive skills), experience and education.

$$E_i = g^* ( G_i^1, edn_i, exp_i, v_{ki} ) + u_i \quad (6)$$

- The quasi-reduced form parameters on *edn* and *exp* now reflect the impact of education and experience on the production of skills other than the observed cognitive skills.

$$9) \frac{\partial g^*}{\partial x} = \frac{\partial f}{\partial G^2} * \frac{\partial h_2}{\partial x} + \frac{\partial f}{\partial G^3} * \frac{\partial h_3}{\partial x}$$

- The difference between the reduced form and quasi-reduced form estimates measures the contribution of the observed skill to the total “return” to schooling

- Taking difference between RF (equation 5) and QRF (equation 9) yields:

$$\frac{\beta_f}{\beta_x} - \frac{\beta_g^*}{\beta_x} = \frac{\beta_f}{\beta_{G^1}} * \frac{\beta_h}{\beta_x} \quad (10)$$

- I.E. the fraction of the impact of schooling S on earnings due to influence of S on literacy skills and their impact on earnings
- Thus comparing coefficient on S in RF earnings eqn to that in QRF eqn measures role of literacy skill generation in impact of schooling on earnings

# DATA: International Adult Literacy and Skills Survey

- IALSS sample size: 23,038
- Drop immigrants, aboriginals, students => 14,666 obs
- Rich data on education (eg years of schooling, attainment, prov of HS), parental characteristics, exact date of birth
- Earnings sample drops self-employed, unemployed, non-participants, wage outliers: 7569 obs
- Correlation among test scores:
  - Prose and Document .96
  - Document and Numeracy .92
  - Document and Problem solving .92
- Factor analysis: one principal component placing essentially equal weight on all four scores
- We focus on average score, but report results for individual skills

# Compulsory schooling laws

- We use minimum School Leaving Age (SLA) and maximum School Entry Age (SEA) as IVs for schooling  $S$
- Identification assumes variations in SLA and SEA over time and across provinces induced changes in  $S$  that are unrelated to 'unobserved ability' factors
- Compiled data from provincial statutes and date of proclamation or ascension from provincial regulations
- Note changes often implemented during year (e.g. July 1 or Sept 1)

# Compulsory schooling laws

- Using exact date of birth, province of HS and implementation date allows a more precise match of CSL to affected individuals (compared to previous studies)
- EG can exploit rules that say "until end of June in year turn 16" versus just "16"
- Use main and most basic SLA and SEA when there are exemptions or other requirements
- Use urban SLA and SEA if both urban and rural specified

# Outline of empirical results

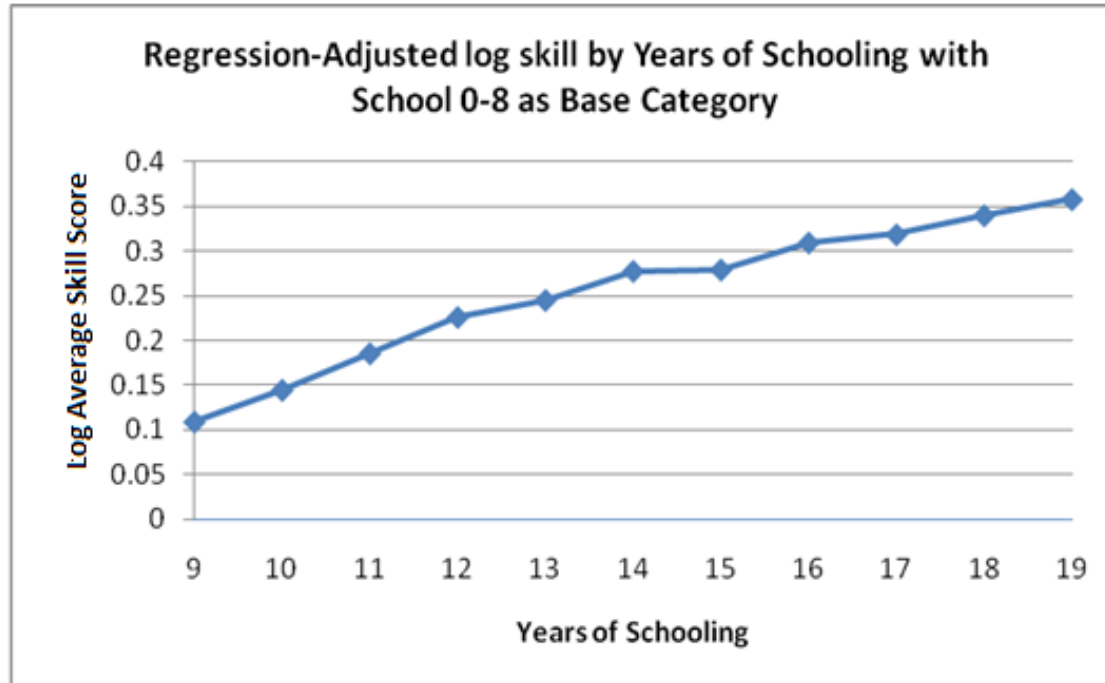
- Evidence on causal impact of schooling on basic literacy and numeracy skills (skill production functions)
- RF and QRF earnings equations, i.e. with and without controls for basic cognitive skills
- Quantile regressions – to see if impacts of education, experience and skills vary across earnings distribution (in Appendix)



# Cognitive skills and schooling

- Figure 1 shows partial relationship controlling for gender, age, age squared, parental characteristics, province, urban/rural
- Slightly concave especially after 16 years
- Diminishing returns not surprising given these are basic skills
- We drop those with  $S > 16$  and specify linear relationship

# Figure 1



# Determinants of skills II

- Table 2a reports log skills regressions using average skill score
- Small gender difference
- Essentially no relationship between skills and age in cross-section (e.g. impact of 1 year at age 30 = - 0.4%, at age 50 = -0.7%)
- G&R (2003) also found no relationship between literacy skills and age or experience with IALS 94 data
- Strong relationship with formal schooling
- Results for individual cognitive skills similar, though sign of gender coefficient varies across skills (Table 2b shows IV estimates)
- Partial impact of S largest for Doc literacy & Numeracy

# Addressing potential omitted variables bias

- Column 2 (OLS2) adds controls for parental characteristics
- Parental education only matters if parents dropouts or parental education unknown (OLS2)
- Other parental influences (occupation, immigrant, mother working) minor
- Column 3 adds proxies for unobserved ability
- Ease of learning mathematics in high school
- Modest declines in coefficient on schooling in columns 2 and 3
- IV1 uses SLA as IV, matched using DOB and province of HS
- IV2 uses SLA and SEA, matched using DOB and province of birth
- First stage results in Table 3

**Table 2a: Log of Average Skill Score Regressions**

Variable	OLS1	OLS2	OLS3	IV1	IV2
Years of Schooling	0.036*** [0.001]	0.031*** [0.001]	0.028*** [0.001]	0.073*** [0.012]	0.084*** [0.012]
Female	-0.012** [0.005]	-0.010** [0.005]	-0.007 [0.005]	-0.024*** [0.007]	-0.027*** [0.007]
Age	0.003*** [0.001]	0.006*** [0.001]	0.006*** [0.001]	-0.001 [0.002]	-0.003 [0.002]
Age Squared	-0.007*** [0.001]	-0.009*** [0.001]	-0.009*** [0.001]	0 [0.003]	0.002 [0.003]
<i>Mother's Education</i>					
Less than High School		-0.040*** [0.006]	-0.043*** [0.006]	-0.008 [0.012]	0.001 [0.013]
Some Post Secondary		0 [0.007]	-0.002 [0.007]	-0.015 [0.010]	-0.019* [0.011]
BA or More		0.012 [0.012]	0.01 [0.011]	0.007 [0.015]	0.005 [0.016]
None Reported		-0.066*** [0.011]	-0.068*** [0.011]	-0.011 [0.019]	0.004 [0.021]

*Father's Education*

Less than High School		-0.026*** [0.007]	-0.024*** [0.007]	0.008 [0.013]	0.017 [0.014]
Some Post Secondary		0.002 [0.008]	0.004 [0.008]	-0.007 [0.010]	-0.009 [0.011]
BA or More		0.018* [0.009]	0.024*** [0.009]	-0.005 [0.014]	-0.011 [0.015]
None Reported		-0.047*** [0.011]	-0.045*** [0.011]	0.005 [0.019]	0.019 [0.020]
Immigrant Mother		0.006 [0.008]	0.005 [0.008]	-0.013 [0.011]	-0.019 [0.012]
Immigrant Father		0.016** [0.008]	0.018** [0.007]	0.004 [0.010]	0 [0.011]
Good Math Grades			0.025*** [0.006]		
Teachers Too Fast			-0.026*** [0.006]		
Observations	12370	12370	12370	12370	12370

# LIML Estimates

- LIML provides small sample correction for bias in TSLS
- Bias especially likely if instruments weak and many over-identifying restrictions
- Results for Yrs schooling coefficient:

## LIML Estimates- Literacy

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Variable	OLS2	IV1	LIML1	IV2	LIML2
Years of Schooling	0.031*** [0.001]	0.073*** [0.012]	0.075*** [0.012]	0.084*** [0.012]	0.096*** [0.017]
Observations	12370	12370	12370	12370	12370

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**Table 3: First Stage Results for Years of Schooling**

Variable	IV1	IV2
CSLA $\geq$ 15 & CSLA $<$ 16	0.630*** [0.113]	0.494*** [0.119]
CSLA $\geq$ 16	0.578*** [0.125]	0.479*** [0.133]
CSEA=5 or 6		0.222 [0.179]
CSEA=7		0.389** [0.173]
Female	0.316*** [0.075]	0.319*** [0.075]
Age	0.162*** [0.012]	0.158*** [0.012]
Age Squared	-0.193*** [0.012]	-0.188*** [0.013]
<i>Mother's Education</i>		
Less than High School	-0.740*** [0.111]	-0.729*** [0.112]
Some Post Secondary	0.361*** [0.117]	0.364*** [0.117]
BA or More	0.135 [0.173]	0.14 [0.172]
None Reported	-1.313*** [0.188]	-1.293*** [0.188]



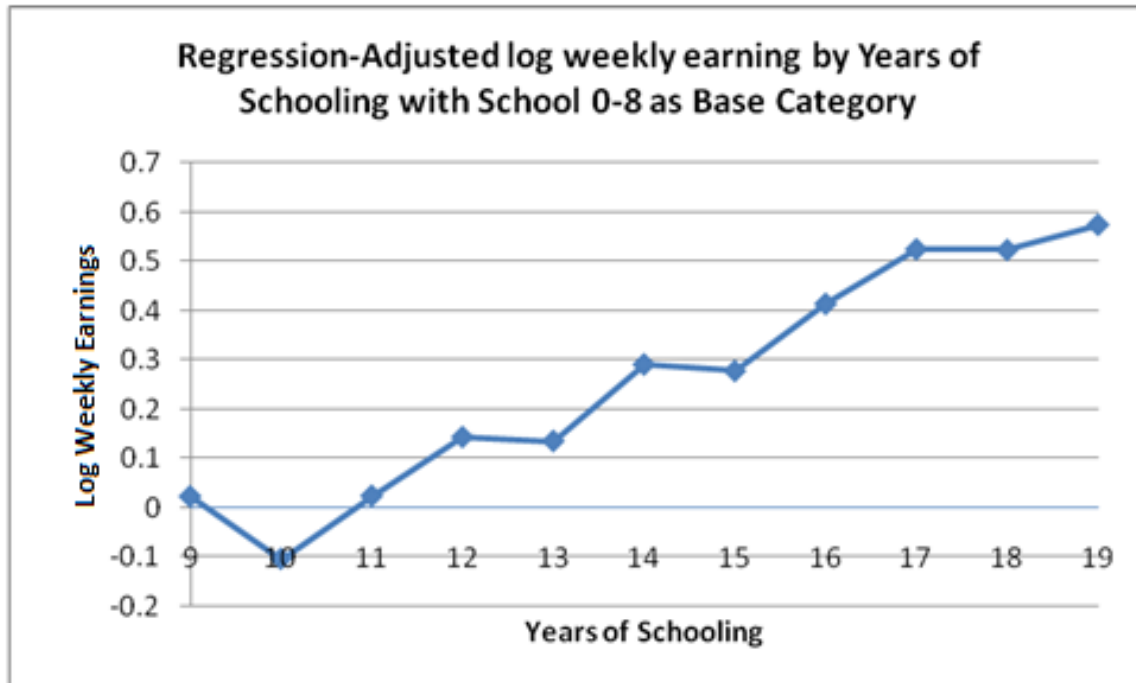
*Father's Education*

Less than High School	-0.809*** [0.109]	-0.818*** [0.109]
Some Post Secondary	0.220* [0.129]	0.207 [0.129]
BA or More	0.564*** [0.147]	0.557*** [0.147]
None Reported	-1.252*** [0.170]	-1.262*** [0.169]
Immigrant Mother	0.446*** [0.123]	0.435*** [0.123]
Immigrant Father	0.241** [0.123]	0.231* [0.123]
Observations	12370	12370
R-squared	0.27	0.27
First Stage F-Statistics	15.8	10.0

# Earnings, schooling and skills

- Earners sample younger, better educated
- IV1 uses SLA and SEA as IV for years of schooling S
- IV2 uses SLA, SEA and province of HS plus province of HS fully interacted with Age as IVs for S and Ave Lit
- Rationale for Prov of HS instrument: Different levels of resources applied to schooling in different provinces for different cohorts will lead to different levels of school quality for otherwise identical individuals
- All regressions include controls for province of residence and urban/rural

# Figure 2



**Table 4: Earnings Regressions**

Variable	OLS1	OLS2	IV1	IV2	IV2
Years of Schooling	0.085*** [0.004]	0.070*** [0.005]	0.089*** [0.026]	0.084*** [0.005]	0.054*** [0.015]
Female	-0.414*** [0.024]	-0.411*** [0.023]	-0.416*** [0.026]	-0.414*** [0.024]	-0.408*** [0.024]
Experience	0.067*** [0.004]	0.066*** [0.004]	0.067*** [0.006]	0.067*** [0.004]	0.065*** [0.004]
Experience Squared	-0.001*** [0.000]	-0.001*** [0.000]	-0.001*** [0.000]	-0.001*** [0.000]	-0.001*** [0.000]
Average Literacy Score		0.003*** [0.000]			0.005** [0.003]
Constant	4.657*** [0.082]	4.115*** [0.115]	4.610*** [0.322]	4.670*** [0.085]	3.548*** [0.553]
Observations	7569	7569	7569	7569	7569
R-squared	0.39	0.41	0.39	0.39	0.39
<i>First Stage F-Statistics</i>					
Years of Schooling			20.4	139.7	139.7
Average Literacy Score					16.8

# LIML estimates

- Overall, very similar to corresponding TSLS estimates:

## LIML Estimates- Earnings

Variable	OLS		IV1	LIML1	IV2		LIML2	
Years of Schooling	0.085*** [0.004]	0.070*** [0.005]	0.089*** [0.026]	0.089*** [0.028]	0.084*** [0.005]	0.054*** [0.015]	0.084*** [0.005]	0.031 [0.039]
Average Literacy Score		0.003*** [0.000]				0.005** [0.003]		0.009 [0.007]
Observations	7569	7569	7569	7569	7569	7569	7569	7569

# Cognitive skills and earnings

- Introducing cognitive skills reduces schooling coefficient by 18% (OLS) to 35% to 40% (IV).
- Since cognitive skills do not increase with age, positive association between earnings and experience must be due to other factors
- Impact of cognitive skills on earnings is substantial. A 25 point increase in skills (half a standard deviation) is associated with an earnings increase equivalent to 1 (OLS) to 2 (IV) extra years of schooling

# Conclusions

- Education has a substantial causal effect on basic literacy and numeracy skills. First evidence of such impacts for adult population.
- IV estimates suggest each year of school raises skills by 7% to 8%, or about  $1/7$  to  $1/6$  of a std deviation
- Indeed, formal schooling is the dominant determinant of these basic cognitive skills
- Finding runs counter to view that family background is key influence
- Parental education has a modest impact, but only matters (if at all) for parents < HS grad

# Conclusions (cont'd)

- Suggests main influence of family background is on amount and quality of schooling, not directly on basic skills
- Basic literacy and numeracy skills account for about 18% (OLS) to 35-40% (IV) of the returns to schooling
- Cognitive skills have substantial effects on earnings: a 25 point increase in skills (1/2 std dev) has impact equivalent to 1 (OLS) to 2 (IV) extra years of schooling



# Appendix

- Individual skill score regressions (Table 2b)
- Quantile regressions

**Table 2b: Individual Skill Score Regressions with CSLA Instrument**

Variable	Log Prose Score	Log Document Score	Log Numeracy Score	Log Problem Solving Score
Years of Schooling	0.070*** [0.012]	0.085*** [0.014]	0.070*** [0.013]	0.069*** [0.012]
Female	0.011 [0.007]	-0.029*** [0.008]	-0.068*** [0.007]	-0.011 [0.007]
Age	0 [0.002]	-0.003 [0.003]	0.001 [0.002]	-0.002 [0.002]
Age Squared	-0.001 [0.003]	0.001 [0.003]	-0.003 [0.003]	0.001 [0.002]
<i>Mother's Education</i>				
Less than High School	-0.003 [0.012]	0.002 [0.014]	-0.011 [0.013]	-0.019 [0.012]
Some Post Secondary	-0.011 [0.010]	-0.026** [0.012]	-0.011 [0.011]	-0.013 [0.010]
BA or More	0.014 [0.015]	-0.002 [0.016]	0.006 [0.019]	0.005 [0.014]
None Reported	0 [0.020]	-0.003 [0.023]	0.007 [0.021]	-0.046** [0.019]

*Father's Education*

Less than High School	0.002 [0.013]	0.012 [0.015]	0.006 [0.015]	0.012 [0.013]
Some Post Secondary	-0.012 [0.010]	-0.005 [0.011]	-0.011 [0.012]	0.001 [0.010]
BA or More	-0.005 [0.014]	-0.006 [0.016]	-0.006 [0.015]	-0.003 [0.014]
None Reported	0.009 [0.020]	0.019 [0.022]	-0.01 [0.022]	0.003 [0.019]
Immigrant Mother	-0.01 [0.011]	-0.019 [0.013]	-0.013 [0.013]	-0.012 [0.012]
Immigrant Father	0.004 [0.010]	0.008 [0.012]	0.002 [0.012]	0 [0.010]
Constant	4.801*** [0.119]	4.690*** [0.138]	4.789*** [0.127]	4.848*** [0.115]
Observations	12370	12370	12370	12370

# Quantile regressions

- Quasi-reduced form earnings equation

$$6) E_i = g^*(G_i^l, yrs_i, exp_i, \theta_i) + \varepsilon_i$$

- Partial derivative of 6) with respect to cognitive skills could vary with unobservables => quantile regressions
- These provide information on derivatives of earnings with respect to observables at different values of unobservables that generate conditional earnings quantiles

# Quantile regressions

- Table 5 shows estimates at 10<sup>th</sup>, 25<sup>th</sup>, 50<sup>th</sup>, 75<sup>th</sup>, 90<sup>th</sup> quantiles
- Returns to schooling and experience decline across quantiles
- Coefficient on skills approximately constant across quantiles
- Suggests cognitive skills do not interact with unobserved abilities or skills in generating earnings

**Table 8: Quantile Earnings Regressions**

	10th Quantile	25th Quantile	Median	75th Quantile	90th Quantile
Female	-0.48*** (0.048)	-0.46*** (0.032)	-0.36*** (0.020)	-0.36*** (0.021)	-0.36*** (0.032)
Years of Schooling	0.079*** (0.011)	0.065*** (0.0065)	0.069*** (0.0041)	0.067*** (0.0042)	0.057*** (0.0069)
Experience	0.088*** (0.0063)	0.084*** (0.0041)	0.059*** (0.0025)	0.050*** (0.0024)	0.042*** (0.0036)
Experience Squared	-0.0015*** (0.0001)	-0.0015*** (0.0001)	-0.001*** (0.0001)	-0.0008*** (0.0001)	-0.0006*** (0.0001)
Average Literacy Score	0.0022*** (0.0007)	0.0032*** (0.0004)	0.0029*** (0.0003)	0.003*** (0.0003)	0.0028*** (0.0005)
Constant	3.33*** (0.19)	3.67*** (0.12)	4.26*** (0.083)	4.62*** (0.079)	5.12*** (0.13)
Observations	7768	7768	7768	7768	7768